



## Carnival Tickets (tickets)

Ringo is at a carnival in Singapore. He has some prize tickets in his bag, which he would like to use at the prize game stall. Each ticket comes in one of  $n$  colours and has a non-negative integer printed on it. The integers printed on different tickets might be the same. Due to a quirk in the carnival rules,  $n$  is guaranteed to be **even**.

Ringo has  $m$  tickets of each colour in his bag, that is a total of  $n \cdot m$  tickets. The ticket  $j$  of the colour  $i$  has the integer  $x[i][j]$  printed on it ( $0 \leq i \leq n - 1$  and  $0 \leq j \leq m - 1$ ).

Game එකෙහි 0 to  $k - 1$  අංක කරන ලද වට  $k$  ගණනකි. සෑම වටයක්ම පහත පරිදි වේ:

- Ringo ඉතිරි **tickets** වලින්, සෑම පාටකින්ම tickets එක බැගින්, tickets  $n$  ප්රමාණයක් game master ට දෙනු ලැබේ.
- මෙම  $a[0], a[1] \dots a[n - 1]$  අංකිත tickets  $n$  ගණනෙහි order(පිළිවෙල) අදාල නැත.
- Game master තමා ගාව ඇති පෙට්ටියකින්(lucky draw box)  $b$  නම් අංකයක් ඇති card එකක් ගනී.
- Game master, 0 to  $n - 1$  දක්වා ඇති, සෑම  $i$  අගයකටම,  $a[i]$  and  $b$  අතර ඇති absolute differences (මාපාංක,  $|a[i] - b|$ ) ගණනය කරයි. ඒවාගේ(මාපාංක අගයන්) එකතුව  $S$  ලෙස ගනී.
- ඔහු, එම  $S$  අගයට සමාන තැග්ගක්, Ringo ට දෙයි.
- මෙම වටයේ භාවිතා කළ tickets ඉවත් කෙරේ.

The remaining tickets in Ringo's bag after  $k$  rounds of the game are discarded(ඉවත් කෙරේ).

By watching closely, Ringo realized that the prize game is rigged(වංචනිකයි)! There is actually a printer inside the lucky draw box. සෑම වටයකදීම game master, තැග්ග( $S$ ) අවම කළ හැකි අගයක් හිතාමතාම  $b$  ලෙස ගනී. The value chosen by the game master is printed on the special card for that round.

මෙම තත්වයන් දැනගෙන, සෑම වටයකදීම ලැබෙන තැග්ග( $S$ ) වල එකතුව උපරිම වන පරිදි Ringo ට, එක් එක් වටයදී, සුදුසු පරිදි ticket තේරිය යුතුය.

## Implementation details

You should implement the following procedure:

```
int64 find_maximum(int k, int[][] x)
```

- $k$ : the number of rounds.
- $x$ : an  $n \times m$  array describing the integers on each ticket. Tickets of each color are sorted in

non-decreasing order of their integers.

- This procedure is called exactly once.
- This procedure should make exactly one call to `allocate_tickets` (see below), describing  $k$  ticket sets, one for each round. The allocation should maximize the total value of the prizes.
- This procedure should return the maximum total value of the prizes.

The procedure `allocate_tickets` is defined as follows:

```
void allocate_tickets(int[][] s)
```

- $s$ : an  $n \times m$  array. The value of  $s[i][j]$  should be  $r$  if the ticket  $j$  of the colour  $i$  is used in the set of round  $r$  of the game, or  $-1$  if it is not used at all.
- For each  $0 \leq i \leq n - 1$ , among  $s[i][0], s[i][1], \dots, s[i][m - 1]$  each value  $0, 1, 2, \dots, k - 1$  must occur exactly once, and all other entries must be  $-1$ .
- If there are multiple allocations resulting in the maximum total prize value, it is allowed to report any of them.

## Examples

### Example 1

Consider the following call:

```
find_maximum(2, [[0, 2, 5], [1, 1, 3]])
```

This means that:

- there are  $k = 2$  rounds;
- the integers printed on the tickets of colour 0 are 0, 2 and 5, respectively;
- the integers printed on the tickets of colour 1 are 1, 1 and 3, respectively.

A possible allocation that gives the maximum total prize value is:

- In round 0, Ringo picks ticket 0 of colour 0 (with the integer 0) and ticket 2 of colour 1 (with the integer 3). The lowest possible value of the prize in this round is 3. E.g., the game master may choose  $b = 1$ :  $|1 - 0| + |1 - 3| = 1 + 2 = 3$ .
- In round 1, Ringo picks ticket 2 of colour 0 (with the integer 5) and ticket 1 of colour 1 (with the integer 1). The lowest possible value of the prize in this round is 4. E.g., the game master may choose  $b = 3$ :  $|3 - 1| + |3 - 5| = 2 + 2 = 4$ .
- Therefore, the total value of the prizes would be  $3 + 4 = 7$ .

To report this allocation, the procedure `find_maximum` should make the following call to `allocate_tickets`:

- `allocate_tickets([[0, -1, 1], [-1, 1, 0]])`

Finally, the procedure `find_maximum` should return 7.

## Example 2

Consider the following call:

```
find_maximum(1, [[5, 9], [1, 4], [3, 6], [2, 7]])
```

This means that:

- there is only one round,
- the integers printed on the tickets of colour 0 are 5 and 9, respectively;
- the integers printed on the tickets of colour 1 are 1 and 4, respectively;
- the integers printed on the tickets of colour 2 are 3 and 6, respectively;
- the integers printed on the tickets of colour 3 are 2 and 7, respectively.

A possible allocation that gives the maximum total prize value is:

- In round 0, Ringo picks ticket 1 of colour 0 (with the integer 9), ticket 0 of colour 1 (with the integer 1), ticket 0 of colour 2 (with the integer 3), and ticket 1 of colour 3 (with the integer 7). The lowest possible value of the prize in this round is 12, when the game master chooses  $b = 3$ :  $|3 - 9| + |3 - 1| + |3 - 3| + |3 - 7| = 6 + 2 + 0 + 4 = 12$ .

To report this solution, the procedure `find_maximum` should make the following call to `allocate_tickets`:

- `allocate_tickets([[-1, 0], [0, -1], [0, -1], [-1, 0]])`

Finally, the procedure `find_maximum` should return 12.

## Constraints

- $2 \leq n \leq 1500$  and  $n$  is even.
- $1 \leq k \leq m \leq 1500$
- $0 \leq x[i][j] \leq 10^9$  (for all  $0 \leq i \leq n - 1$  and  $0 \leq j \leq m - 1$ )
- $x[i][j - 1] \leq x[i][j]$  (for all  $0 \leq i \leq n - 1$  and  $1 \leq j \leq m - 1$ )

## Subtasks

1. (11 points)  $m = 1$
2. (16 points)  $k = 1$
3. (14 points)  $0 \leq x[i][j] \leq 1$  (for all  $0 \leq i \leq n - 1$  and  $0 \leq j \leq m - 1$ )
4. (14 points)  $k = m$
5. (12 points)  $n, m \leq 80$
6. (23 points)  $n, m \leq 300$

7. (10 points) No additional constraints.

## Sample grader

The sample grader reads the input in the following format:

- line 1:  $n \ m \ k$
- line  $2 + i$  ( $0 \leq i \leq n - 1$ ):  $x[i][0] \ x[i][1] \ \dots \ x[i][m - 1]$

The sample grader prints your answer in the following format:

- line 1: the return value of `find_maximum`
- line  $2 + i$  ( $0 \leq i \leq n - 1$ ):  $s[i][0] \ s[i][1] \ \dots \ s[i][m - 1]$